

**Elective - II : Digital Signal Processing**

P. Pages : 2

Time : Three Hours



TKN/KS/16/7657

Max. Marks : 80

- Notes :
1. All questions carry marks as indicated.
  2. Solve Question 1 OR Questions No. 2.
  3. Solve Question 3 OR Questions No. 4.
  4. Solve Question 5 OR Questions No. 6.
  5. Solve Question 7 OR Questions No. 8.
  6. Solve Question 9 OR Questions No. 10.
  7. Solve Question 11 OR Questions No. 12.
  8. Due credit will be given to neatness and adequate dimensions.

1. a) Given the discrete time signal  $x(n) = n$  for  $-3 \leq n \leq 2$ . 6  
 $x(n) = 0$  otherwise  
 sketch i)  $x(n+3)$  ii)  $x(n-2)$  iii)  $x(-n)$
  - b) State Nyquist Sampling Theorem. An analog signal  $x(t) = \sin 480\pi t + 3\sin 720\pi t$  is 7  
 sampled at 600 times / sec.  
 Calculate :  
 i) Nyquist Sampling Rate  
 ii) Folding Frequency  
 iii) What are frequencies in radians in the resulting signal.
- OR**
2. a) Determine whether the following systems are static / dynamic, linear or non linear, time 6  
 invariant or variant. causal or non causal.  
 (a)  $y(n) = \cos x(n)$  (b)  $y(n) = n x(n)$
  - b) The impulse response of LTI system is :  $h(n) = \{2 \underset{\uparrow}{4} \ 6 \ 7\}$  Determine the response of 7  
 the system to the input signal  $x(n) = \{1 \ 2 \ 3 \ 1\}$  using graphical convolution.
3. a) Determine the Fourier Transform and energy density spectrum of the sequence 6  
 $x(n) = A \quad 0 \leq n \leq L-1$   
 $= 0 \quad \text{otherwise}$
  - b) By use of DTFT determine. Convolution of the sequences. 7  
 $x_1(n) = x_2(n) = \{1 \ \underset{\uparrow}{1} \ 1\}$
- OR**
4. a) Determine the DTFT of 6  
 a)  $2^n u(n)$  b)  $x(n) = u(n) - u(n-6)$
  - b) State and prove linearity and time shifting property of DTFT. 7
5. a) Determine the Z transform of  $x(n) = \left(\frac{1}{2}\right)^n \mu(n) + \left(\frac{1}{3}\right)^n \mu(n)$  showing ROC. 7

b) Prove the time shifting property and differentiation property of Z transform. 7

**OR**

6. a) Determine the inverse Z transform of the following X(Z) by the partial fraction expansion method. 9

$$x(z) = \frac{1}{1 - 1.5z^{-1} + 0.5z^{-2}}$$

if ROC i)  $|Z| > 1$                       ii)  $|Z| < 0.5$

iii)  $0.5 < |Z| < 1$

b) What is region of conversion? Explain. 5

7. Obtain the direct form I, direct form II. Cascade and parallel structures for 13

$$y(n) = \frac{3}{4}y(n) - \frac{1}{8}y(n-2) + x(n) + \frac{1}{3}x(n-1)$$

**OR**

8. a) Obtain direct form and cascade form realisation for the transfer function of an FIR system given by 10

$$H(Z) = \left(1 - \frac{1}{4}Z^{-1} + \frac{3}{8}Z^{-2}\right) \left(1 - \frac{1}{8}Z^{-1} - \frac{1}{2}Z^{-2}\right)$$

b) What all pass systems and minimum phase systems? 3

9. a) Design digital filter using bilinear transformation for following analog filter. 6

$$H(S) = \frac{2}{(S+1)(S+3)} \text{ with } T_s = 0.1 \text{ sec.}$$

b) For the analog transfer function determine H(Z) using impulse invariance technique 7  
 $T_s = 1 \text{ sec.}$

$$H(S) = \frac{1}{(S+1)(S+2)}$$

**OR**

10. The Specifications of desired low pass filter is : 13

$$0.8 \leq |H(\omega)| \leq 1 \qquad 0 \leq \omega \leq 0.2\pi$$

$$|H(\omega)| \leq 0.2 \qquad 0.32\pi \leq \omega \leq \pi$$

Design Butterworth digital filter using impulse invariance method.

11. Given  $x(n) = \{1 \ 2 \ 3 \ 4 \ 4 \ 3 \ 2 \ 1\}$  find X(K) using DIT FFT algorithm. 14

**OR**

12. a) Find DFT of  $\{1 \ 2 \ 3 \ 4\}$ . 5

b) Compute circular convolution of 9

$$\{1 \ 2 \ 1 \ 2\} \quad \{1 \ 2 \ 3 \ 4\}$$

Using DFT & IDFT.

\*\*\*\*\*