

**Applied Mathematics - IV**

**Paper - I**

P. Pages : 3

Time : Three Hours



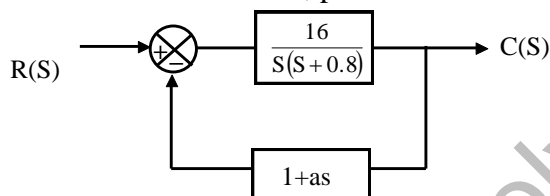
**TKN/KS/16/7366**

Max. Marks : 80

- Notes :
1. All questions carry marks as indicated.
  2. Solve Question 1 OR Questions No. 2.
  3. Solve Question 3 OR Questions No. 4.
  4. Solve Question 5 OR Questions No. 6.
  5. Solve Question 7 OR Questions No. 8.
  6. Solve Question 9 OR Questions No. 10.
  7. Solve Question 11 OR Questions No. 12.
  8. Use of non programmable calculator is permitted.

1. a) Define : 6  
 i) Step signal ii) Ramp signal  
 iii) Parabolic signal and  
 Find their laplace transform.

- b) For a system shown below, find the value of 'a' such that the damping ratio is 0.5. 6  
 Determine the rise time, peak time in the unit step response.



**OR**

2. a) Discuss time response of a general second order system in a unit step input. 6  
 b) Define transfer function and obtain it for series R-C circuit. 6

3. a) If  $z\{f(n)\} = f(z)$  then prove that  $z\{f(n+k)\} = z^k \left[ F(z) - \sum_{i=0}^{k-1} f(i)z^{-i} \right]$  for  $k > 0$ . 6

- b) Find z-Transform of  $\frac{(k+1)(k+2)}{2!} a^k$  6

**OR**

4. a) Find inverse z-transform of  $\frac{3z^2 + 2z + 1}{z^2 - 3z + 2}$  6

- b) Solve the difference equation  $y_{n+2} + 6y_{n+1} + 9y_n = 2^n$  given  $y_0 = 0 = y_1$ . 6

5. a) Define : 6  
 i) Fuzzy set  
 ii)  $\alpha$  - level set  
 iii) Normalized fuzzy set.

- b) If  $X = \{x_1, x_2, x_3\}$ ,  $Y = \{y_1, y_2, y_3\}$  The fuzzy set A of X, fuzzy set B of Y are defined as 6  
 follows :  
 $A = \{0.2/x_1, 0.3/x_2, 0.5/x_3\}$   
 $B = \{0.5/y_1, 0.6/y_2, 0.7/y_3\}$   
 Then Find  $A \times B$ .

**OR**

6. a) If fuzzy sets are - 6  
 $A = \frac{0.3}{30} + \frac{0.7}{60} + \frac{1}{100}$ ,  $B = \frac{0.2}{20} + \frac{0.4}{40} + \frac{0.6}{60}$ ,  $C = \frac{0.3}{50} + \frac{0.6}{100}$   
 Find fuzzy relation  $R = A \times B$ ,  $S = B \times C$ . Also find  $R \cup S$ .

- b) Given the membership function for the fuzzy sets A, B and C as 6  
 $\mu_A(x) = \frac{x}{x+2}$ ,  $\mu_B(x) = 2^{-x}$  and  $\mu_C(x) = \frac{1}{1+10(x-2)^2}$

Where  $x = \{0, 1, 2, 3, 4, 5\}$  Plot the graph  $\mu_A, \mu_B$  and  $\mu_C$  check whether

- i)  $A \cup (\bar{A} \cap B) = A \cup B$   
 ii)  $A \cap \bar{A} = \phi$

7. a) Find the root of the equation  $x + \log_{10}^x - 3.375 = 0$  correct upto three decimal places. 6  
 Using Newton Raphson method.

- b) Apply Crout's method to solve the equations : 6  
 $3x + 2y + 7z = 4$   
 $2x + 3y + z = 5$   
 $3x + 4y + z = 7$

**OR**

8. a) Find the root of  $e^x - 4x = 0$  by Regula falsi method correct upto third decimal place. 6

- b) Solve by Gauss - Seidal method 6  
 $2x - 3y + 20z = 25$   
 $20x + y - 2z = 17$   
 $3x + 20y - z = -18$

9. a) Using Euler's modified method solve  $\frac{dy}{dx} = x + y$  for  $x = 0.1$ , given that  $y(0) = 1$ ,  $h = 0.05$ . 7

- b) Use Runge Kutta method to find approximate value of  $y$  for  $x = 0.2$  when  $\frac{dy}{dx} = xy + y^2$  given  $y(0) = 1, h = 0.1$ . 7

**OR**

10. a) Use Milne's predictor correction method to find  $y(0.4)$  from  $\frac{dy}{dx} = 1 + xy^2$  7  
 $y(0) = 1, y(0.1) = 1.105, y(0.2) = 1.223, y(0.3) = 1.355$

- b) Solve  $\frac{dy}{dx} = yz + x, \frac{dz}{dx} = xz + y$  for  $x = 0.2$  given  $y(0) = 1, z(0) = -1$ , by Runge Kutta method upto 3 decimals. 7

11. a) A random variable  $X$  has density function 6  
 $f(x) = kx^2 \quad 1 \leq x \leq 2$   
 $= kx \quad 2 < x < 3$   
 $= 0 \quad \text{otherwise}$

Find the constant  $k$  and the distribution function.

- b) Find the mean, median and mode for a random variable  $x$  having probability density function 6  
 $f(x) = 4x(1-x^2) \quad 0 < x < 1$   
 $= 0 \quad \text{otherwise}$

- c) Find moment generating function of a random variable 6  
 $X = \frac{1}{2} \text{ Prob } \frac{1}{2}$   
 $= -\frac{1}{2} \text{ Prob } \frac{1}{2}$

Also find first four moments about origin.

**OR**

12. a) Find the probability of getting between 2 heads to 4 heads in 10 tosses of fair coin using normal distribution. 6

- b) Find the coefficient of 6  
 i) skewness and ii) kurtosis of distribution  
 $f(x) = 4x(9-x^2)/81 \quad 0 < x \leq 3$   
 $= 0 \quad \text{otherwise}$

- c) Can the function  $f(x) = c(1-x^2) \quad 0 \leq x \leq 1$  6  
 $= 0 \quad \text{otherwise}$   
 be a distribution function ? Explain.

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